

Name: _____
Unit 9 Review

Date: _____
WS #24

Calc. # _____
Period: _____

**1 – 8. Simplify the following without the use of your calculator.
Express answers in a + bi form (where necessary):**

1. i^9

2. $i^{12} \cdot i^{15}$

3. $2\sqrt{-108}$

4. $2\sqrt{-28} + \sqrt{-63}$

5. $(3 + 2i) + (-3 + 5i) - (1 + 4i)$

6. $(x - 5i)^2$

7. $(3x - 4i)(3x + 4i)$

8. $3i(1 - 2i)^2$

9. $x^2 + 5x + 3 = 7x - 2$

10. $x^2 + 13x + 25 = 5x$

9 – 12. Solve the following equations and express the answers in a + bi form:

11. $2x^2 = -2(3x + 6)$

12. $\frac{6 + 2x}{x} = \frac{x - 2}{-2}$

13. Determine all values of k that would result in the equation $x^2 + 6x + k = 0$ having real, rational and equal roots (double roots).

14. Find the value(s) of k for which the equation $2x^2 + 8x + k = 0$ has imaginary roots.

15. Find the value(s) of k for which the equation $x^2 + (k - 4)x + 4 = 0$ has imaginary roots.

16. Show that the product of $(3 + 2i)$ and its conjugate would be a purely real number.

NOW YOU TRY!

1 – 12. Simplify the following without the use of your calculator. Express answers in $a + bi$ form (where necessary):

1. i^{25}

2. $i^{15} \cdot i^{30}$

3. $(3 - 6i)^2$

4. $\sqrt{-192}$

5. $(2 - \sqrt{-81}) + (-3 + \sqrt{-49})$

6. $7\sqrt{-12} - \sqrt{-48}$

7. $(4 + 5i) - (6i - 3) - (2 + 4i)$

8. $(x - 2i)^2$

9. $(4i)^3 + (9 - i)^2$

10. $4i(3 - 2i)^2$

11. $(x - 3i)(x + 3i)$

12. $2xi(5 - 4i)$

13 – 16. Solve the following equations and express the answers in $a + bi$ form:

13. $6x^2 + 3 = 8x$

14. $3x^2 = -2(2x + 3)$

15. $2x^2 + 5 = 6x$

16. $\frac{-2+3x}{x} = \frac{x+4}{2}$

17. What is value of k for which $3x^2 - 6x + k = 0$ has real roots?

18. What is the smallest integer value of k that makes the roots of $x^2 - kx + 4 = 0$ imaginary?

19. Which value of k will make the roots of $2x^2 - 4x + k = 0$ imaginary?

20. Find the value of k for which the $kx^2 - 8x - 2 = 0$ has "double" roots.

21. Find the value(s) of k for which the $2x^2 + (k - 2)x + 2 = 0$ has imaginary roots.

1-8. Simplify the following without the use of your calculator.
Express answers in a + bi form (where necessary):

1. $i^{19} = i^5 = i$
 $(i^2)^{9.5} = (-1)^{9.5} = -i$

2. $i^{12} \cdot i^{15} = i^{27} = i^3 = -i$
 $(i^2)^{13.5} = (-1)^{13.5} = -i$

3. $2\sqrt{-108} = 2\sqrt{36 \cdot 3 \cdot (-1)} = 12\sqrt{3}(-1) = -12\sqrt{3}$

4. $2\sqrt{-28} + \sqrt{-63} = 2\sqrt{7 \cdot 4 \cdot (-1)} + \sqrt{9 \cdot 7 \cdot (-1)} = 4i\sqrt{7} + i\sqrt{7} = 5i\sqrt{7}$

5. $(3+2i) + (-3+5i) = (-1+4i)$

6. $(x-5)^2 = (x-5)(x-5) = x^2 - 5xi - 5xi + 25 = x^2 - 10xi + 25$

7. $(3x-4i)(3x+4i) = 9x^2 + 12xi - 12xi - 16(i^2) = 9x^2 + 16$

8. $3i(1-2i)^2 = 3i(1-2i)(1-2i) = 3i(1-2i-2i+4i^2) = 3i(1-3-4i) = 3i(-2-4i) = -6i-12i^2 = 12-6i$

9-12. Solve the following equations and express the answers in a + bi form:

9. $x^2 + 5x + 3 = 7x - 2$
 $x^2 - 2x + 5 = 0$
 $x = \frac{2 \pm \sqrt{(-2)^2 - 4(1)(5)}}{2(1)} = \frac{2 \pm \sqrt{4-20}}{2} = \frac{2 \pm \sqrt{-16}}{2} = \frac{2 \pm 4i}{2} = 1 \pm 2i$

10. $x^2 + 13x + 25 = 5x$
 $x^2 + 8x + 25 = 0$
 $x = \frac{-8 \pm \sqrt{8^2 - 4(1)(25)}}{2(1)} = \frac{-8 \pm \sqrt{64-100}}{2} = \frac{-8 \pm \sqrt{-36}}{2} = \frac{-8 \pm 6i}{2} = -4 \pm 3i$

11. $2x^2 = -2(3x+6)$
 $2x^2 = -6x - 12$
 $2x^2 + 6x + 12 = 0$
 $x = \frac{-6 \pm \sqrt{6^2 - 4(2)(12)}}{2(2)} = \frac{-6 \pm \sqrt{36-96}}{4} = \frac{-6 \pm \sqrt{-60}}{4} = \frac{-6 \pm \sqrt{4 \cdot 15 \cdot (-1)}}{4} = \frac{-6 \pm 2i\sqrt{15}}{4} = \frac{-3 \pm i\sqrt{15}}{2}$

12. $\frac{6+2x}{x} \neq \frac{x-2}{-2}$
 $-12-4x = x^2 - 2x + 12$
 $0 = x^2 + 2x + 12$
 $x = \frac{-2 \pm \sqrt{2^2 - 4(1)(12)}}{2(1)} = \frac{-2 \pm \sqrt{4-48}}{2} = \frac{-2 \pm \sqrt{-44}}{2} = \frac{-2 \pm 2i\sqrt{11}}{2} = -1 \pm i\sqrt{11}$

13. Determine all values of k that would result in the equation $x^2 + 6x + k = 0$ having real, rational and equal roots (double roots).

$(b)^2 = 4(1)(k) = 0$
 $36 - 4k = 0$
 $-4k = -36$
 $k = 9$

14. Find the value(s) of k for which the equation $2x^2 + 8x + k = 0$ has imaginary roots.

$(8)^2 = 4(2)(k) < 0$
 $64 - 8k < 0$
 $-8k < -64$
 $k > 8$

15. Find the value(s) of k for which the equation $x^2 + (k-4)x + 4 = 0$ has imaginary roots.

$(k-4)^2 = 4(1)(4) < 0$
 $(k-4)(k-4) - 16 < 0$
 $k^2 - 4k - 4k + 16 - 16 < 0$
 $k^2 - 8k < 0$
 $k(k-8) < 0$
 $0 < k < 8$

16. Show that the product of $(3+2i)$ and its conjugate would be a purely real number.

$(3+2i)(3-2i) = 9 - 4i^2 = 9 - 4(-1) = 9 + 4 = 13$

NOW YOU TRY!

1-12. Simplify the following without the use of your calculator. Express answers in a + bi form (where necessary):

1. $i^{15} \cdot i^{20.5}$
 $i^5 \cdot i^{20.5}$
 $i^5 \cdot i^{20}$
 $i^5 \cdot 1$
 i^5

2. $i^{15} \cdot i^{30}$
 $i^5 \cdot i^{30}$
 $i^5 \cdot 1$
 i^5

3. $(3-6i)^2$
 $(3-6i)(3-6i)$
 $9-18i-18i+36i^2$
 $9-36i-36$
 $-27-36i$

5. $(2-\sqrt{-81})+(-3+\sqrt{-49})$
 $(2-9i)+(-3+7i)$
 $-1-2i$

6. $7\sqrt{-12}-\sqrt{-48}$
 $7\sqrt{3(-1)}-\sqrt{16(3)(-1)}$
 $7i\sqrt{3}-4i\sqrt{3}$
 $3i\sqrt{3}$

4. $\sqrt{-192}$
 $\sqrt{64 \cdot 3 \cdot -1}$
 $8i\sqrt{3}$

7. $(4+5i)-(6i-3)-(2+4i)$
 $4+5i-6i+3-2-4i$
 $5-5i$

8. $(x-2i)^2$
 $(x-2i)(x-2i)$
 $x^2-2xi-2xi+4i^2$
 $x^2-4xi-4$

9. $(4i)^3 + (9-i)^2$
 $64i^3 + (9-i)(9-i)$
 $64(-i)^3 + 81-9i-9i+i^2$
 $64(-1)(-i) + 80-18i$
 $64i + 80 - 18i = 80 + 46i$

11. $(x-3i)(x+3i)$
 $x^2 + 3xi - 3xi - 9i^2$
 $x^2 + 9$

12. $2xi(5-4i)$
 $10xi - 8xi^2$
 $10xi + 8x$

10. $4i(3-2i)^2$
 $4i(3-2i)(3-2i)$
 $4i(9-6i-6i+4i^2)$
 $4i(5-12i)$
 $20i - 48i^2 = 48 + 20i$

13-16. Solve the following equations and express the answers in a + bi form:

13. $6x^2 + 3 = 8x$
 $-6x^2 - 8x + 3 = 0$

$6x^2 \pm 8x + 3 = 0$
 $x = \frac{-8 \pm \sqrt{64 - 4(6)(3)}}{2(6)} = \frac{-8 \pm \sqrt{64 - 72}}{12} = \frac{-8 \pm \sqrt{-8}}{12}$
 $= \frac{-8 \pm 2i\sqrt{2}}{12} = \frac{-4 \pm i\sqrt{2}}{6}$

14. $3x^2 = -2(2x+3)$
 $3x^2 = -4x - 6$
 $3x^2 + 4x + 6 = 0$
 $x = \frac{-4 \pm \sqrt{16 - 4(3)(6)}}{2(3)} = \frac{-4 \pm \sqrt{16 - 72}}{6} = \frac{-4 \pm \sqrt{-56}}{6}$
 $= \frac{-4 \pm \sqrt{4(-14)}}{6} = \frac{-4 \pm 2i\sqrt{14}}{6} = \frac{-2 \pm i\sqrt{14}}{3}$

15. $2x^2 + 5 = 6x$
 $-2x^2 - 6x + 5 = 0$
 $x = \frac{6 \pm \sqrt{36 - 4(-2)(5)}}{2(-2)} = \frac{6 \pm \sqrt{36 + 40}}{-4} = \frac{6 \pm \sqrt{76}}{-4} = \frac{6 \pm 2\sqrt{19}}{-4} = \frac{-3 \pm \sqrt{19}}{2}$

$x = \frac{4 \pm \sqrt{16 - 4(2)(5)}}{2(2)} = \frac{4 \pm \sqrt{16 - 40}}{4} = \frac{4 \pm \sqrt{-24}}{4} = \frac{4 \pm 2i\sqrt{6}}{4} = \frac{2 \pm i\sqrt{6}}{2}$

$x^2 - 2x + 4 = 0$
 $x = \frac{2 \pm \sqrt{4 - 4(1)(4)}}{2(1)} = \frac{2 \pm \sqrt{4 - 16}}{2} = \frac{2 \pm \sqrt{-12}}{2} = \frac{2 \pm 2i\sqrt{3}}{2} = 1 \pm i\sqrt{3}$

17. What is value of k for which $3x^2 - 6x + k = 0$ has real roots?
 $(-6) \pm \sqrt{36 - 4(3)(k)} \geq 0$
 $36 - 12k \geq 0$
 $-12k \geq -36$
 $k \leq 3$

18. What is the smallest integer value of k that makes the roots of $x^2 - kx + 4 = 0$ imaginary?
 $(-k) \pm \sqrt{k^2 - 4(1)(4)} < 0$
 $k^2 - 16 < 0$
 $(k+4)(k-4) < 0$
 $-4 < k < 4$
 $k = -3$

19. Which value of k will make the roots of $2x^2 - 4x + k = 0$ imaginary?
 $(-4) \pm \sqrt{16 - 4(2)(k)} < 0$
 $16 - 8k < 0$
 $-8k < -16$
 $k > 2$

20. Find the value of k for which the $kx^2 - 8x - 2 = 0$ has "double" roots.
 $(-8) \pm \sqrt{64 - 4(k)(-2)} = 0$
 $64 + 8k = 0$
 $8k = -64$
 $k = -8$

21. Find the value(s) of k for which the $2x^2 + (k-2)x + 2 = 0$ has imaginary roots.
 $(k-2) \pm \sqrt{(k-2)^2 - 4(2)(2)} < 0$
 $(k-2)(k-2) - 16 < 0$
 $k^2 - 2k - 2k + 4 - 16 < 0$
 $k^2 - 4k - 12 < 0$
 $(k-6)(k+2) < 0$
 $k = 6$ or $k = -2$
 $-2 < k < 6$